



**IECON 2021**

47<sup>th</sup> Annual Conference of the  
IEEE Industrial Electronics Society

OCTOBER 13 - 16, 2021 | VIRTUAL CONFERENCE

# Electric Vehicle Smart Charging to Maximize Renewable Energy Usage in a Single Residence

**Georgia  
Tech**



CREATING THE NEXT

Kartik V. Sastry <sup>1</sup>, Prof. Thomas F. Fuller <sup>2</sup>, Prof. Santiago Grijalva <sup>1</sup>,  
Prof. David G. Taylor <sup>1</sup>, Prof. Michael J. Leamy <sup>3</sup>

<sup>1</sup>School of Electrical and Computer Engineering, Georgia Tech, Atlanta, Georgia, USA

<sup>2</sup>School of Chemical and Biomolecular Engineering, Georgia Tech, Atlanta, Georgia, USA

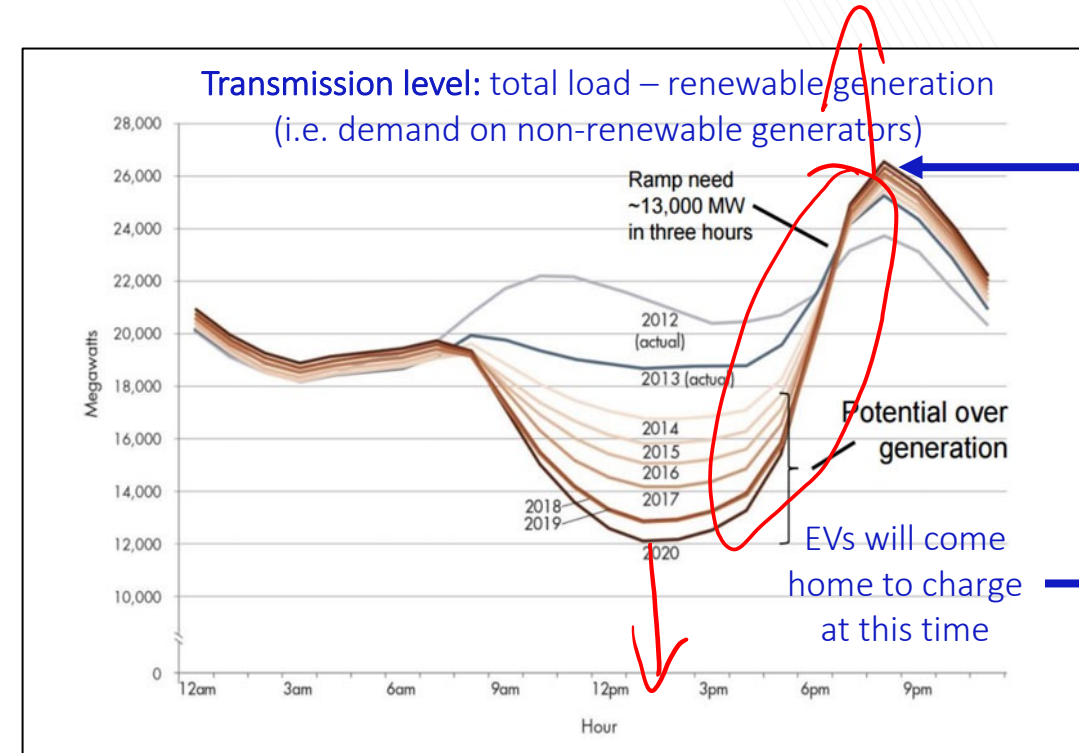
<sup>3</sup>School of Mechanical Engineering, Georgia Tech, Atlanta, Georgia, USA

Sponsor: Georgia Tech Strategic Energy Institute



# Introduction

- Smart charging is motivated by grid-level issues
  - Transmission level: duck curve
  - Distribution level: demand of EVs → overloading, low power quality
  - As EV adoption increases, battery charging load becomes significant
  - Smart charging: *control* battery charging load over time
- Stakeholders
  - EV owners should see benefits in exchange for their participation
  - Power utility should have operational constraints met, plan for capital investments
  - Policy makers should understand what technologies to invest in
- Decentralized smart charging is attractive - will scale well
  - EVs/ homes and the power utility exchange information
  - EVs / homes make *their own* charging decisions
  - Centralized: utility dictates how and when *all* EVs charge



The Duck Curve

Image Source: <https://www.nuscalepower.com/environment/renewables/the-duck-curve>

# Scope of our Study, Contributions



- **Literature review**
  - Most studies consider a *single* objective function. Choice of objective functions varies due to multi-stakeholder nature (Kong, 2016) (Nimalsiri, 2020)
  - Few studies balance one EV owner-centric, one utility-centric objective (Das, 2020) (Das, 2021)
  - **Gap:** Interests of EV owners (and the utility) may not be represented well by a single objective function
  - **Gap:** Utilization of renewable energy is not often considered
- We adopt an EV owner-Centric viewpoint to limit scope
- **Our contributions (focus of this presentation)**
  - Introduced renewable energy consumption as a smart charging objective
  - Developed a framework for multi-objective smart charging in a single residence
    - How to formulate and solve the smart charging problem
    - How to reveal tradeoffs inherent to the problem
  - We believe that this is the most comprehensive treatment of EV owner-centric smart charging to date

Objective functions from the smart charging literature

Utility/Grid-Centric	EV Owner-Centric
Load profile flattening	Maximize convenience
Minimize transmission loss	Maximize fairness
Maximize utilization	Minimize battery degradation
Maximize profit	Minimize charging costs
Regulate power quality	Maximize profit from grid services

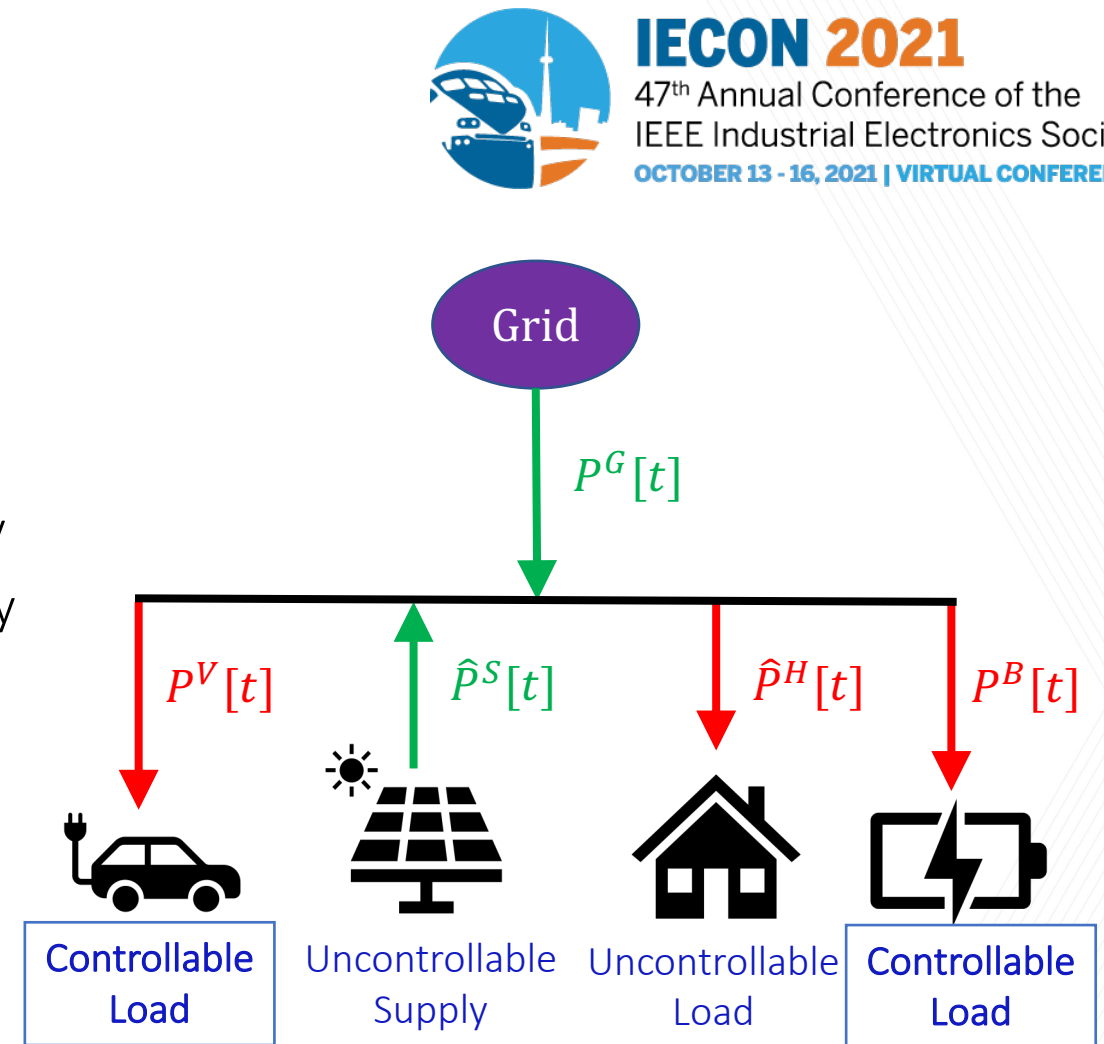
# Details: Home Model

- $P^G[t]$  [kW]: Net power flow *from* grid
- $\hat{P}^H[t]$  [kW]: Estimated power flow *into* home
- $\hat{P}^S[t]$  [kW]: Estimated power flow *from* local solar
- $P^V[t]$  [kW]: Controlled power flow *into* vehicle battery
- $P^B[t]$  [kW]: Controlled power flow *into* storage battery

- Power balance (assume lossless interconnection):

$$P^G[t] + \hat{P}^S[t] = P^V[t] + P^B[t] + \hat{P}^H[t]$$

- Variations:
  - Bidirectional power flow (dis)allowed with grid
  - Bidirectional power flow (dis)allowed with EV
  - Bidirectional power flow (dis)allowed with storage battery
  - No storage battery / solar panel present



**Smart charging:** Determine the 'best' way to (dis)charge the controllable devices over time

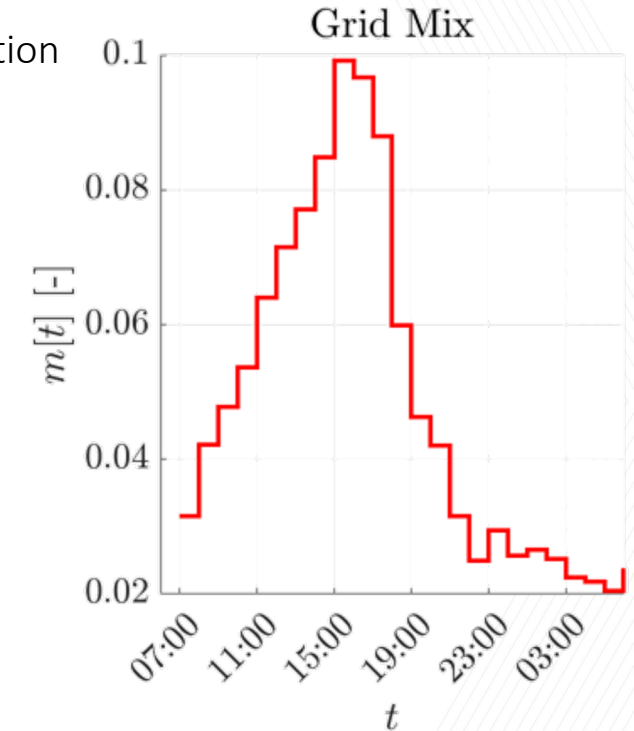




# Utilization of Renewable Energy



- Utilization of renewable energy should be considered as a smart charging objective
  - Environmentally-conscious EV owners may want to maximize their renewable energy consumption
  - Utilities may want to incentivize EV owners to do this. If many EV owners opt-in:
    - Less concern about over-generation around mid-day
    - Utilities can rely more on renewable sources (less on fossil sources!)
- Maximizing renewable energy consumption in a home:
  - Utilities purchase power from several generating resources, including renewable sources
    - Utilities can keep track of the “grid mix” and broadcast this information (e.g.  $m[t]$ )
    - Broadcast can leverage existing infrastructure used for time-of-use price signals
  - Homeowners *can never* know the origins of the electrons flowing into their home
  - *But* homeowners *can* rely more on the grid when the grid is fed by renewable sources!



Example grid mix signal from electric utility in Atlanta, GA

$$\text{Grid Mix} = \frac{\text{Power output from renewable sources}}{\text{Power output from all sources}}$$

Consider the smart charging objective:

Decision variables  $P^V[t], P^B[t]$

Easy to account for local solar (zero if none present)

$$\text{minimize}_{P^V[t], P^B[t]} \sum_{t=1}^{T-1} \underbrace{[m[t]P^G[t] + \hat{P}^S[t]]}_{\text{renewable "supply"}} - \underbrace{(\hat{P}^H[t] + P^V[t] + P^B[t])}_{\text{Total demand (house + charging)}}$$

# Multi-Objective Smart Charging



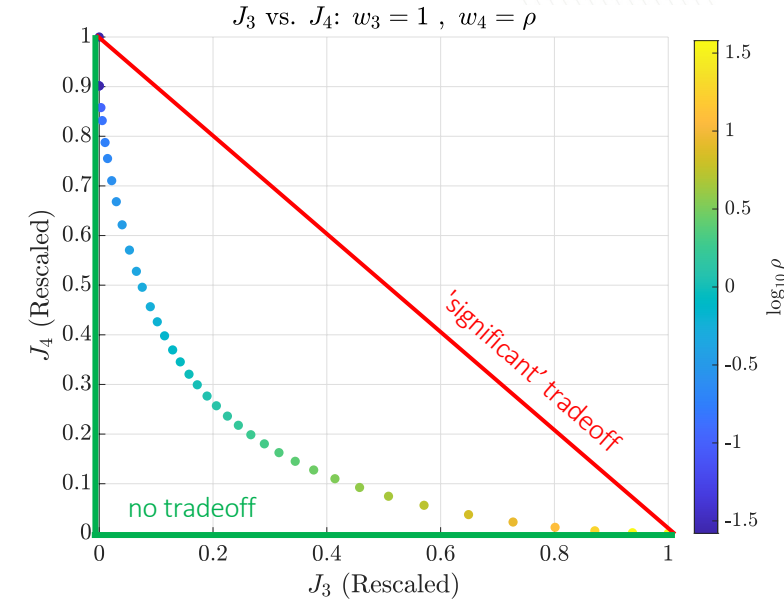
- EV owners probably have multiple objectives which they might expect to *simultaneously* achieve
  - Examples:** maximize renewable energy consumption, charge as fast as possible, minimize battery degradation
  - Represent each objective with a functional (to be minimized):  $J_1, \dots, J_N$

- Natural formulation:

$$\underbrace{\text{minimize}}_{P^V, P^B} \begin{bmatrix} J_1(P^V, P^B) \\ \vdots \\ J_N(P^V, P^B) \end{bmatrix} \quad \text{subject to: } \begin{cases} \text{Power balance} \\ \text{Power/energy upper/lower bounds} \\ \text{Battery dynamics} \\ \text{Initial/final battery energy levels} \end{cases}$$

- All objectives cannot be simultaneously minimized  $\Rightarrow$  *Pareto optimality*
  - At a Pareto optimal solution: performance improvements in one objective can only be achieved by *sacrificing* performance in another objective
  - Inherent tradeoffs in the problem revealed by *set of all* Pareto optimal solutions
  - EV owners should be informed of these tradeoffs!

- For *any* choice of positive weights, minimize  $\sum_{n=1}^N w_n J_n$  yields a Pareto optimal solution to the above problem *if*  $J_1, \dots, J_N$  are all **convex**
  - Revealing tradeoffs: Solve *many* instances of above problem, vary  $w_1, \dots, w_N$
  - Convex formulation makes revealing tradeoffs computationally feasible



Visualization of a Pareto frontier in the “objective-space”. Axes are rescaled using min./max. values. Here:

$$J_3 = \sum_{t=1}^{T-1} t P^V[t] \quad J_4 = \sum_{t=1}^{T-1} (P^V[t])^2 + (P^B[t])^2$$

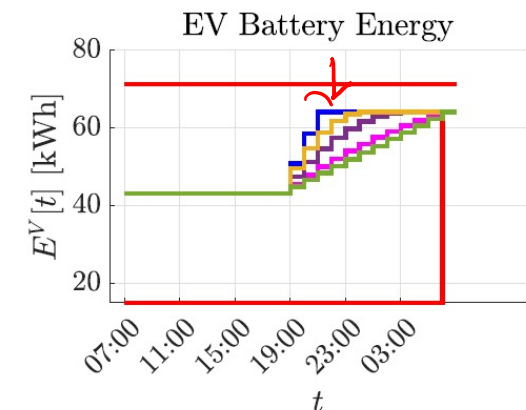
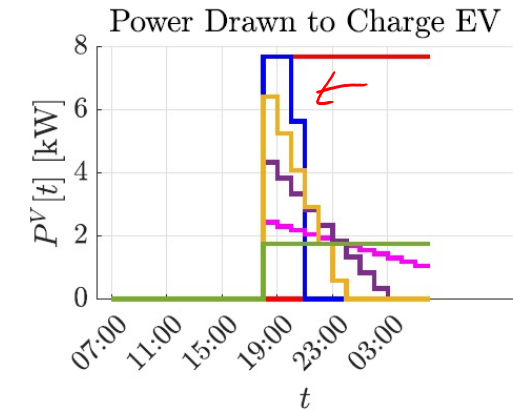
(charge quickly) (charge gently)

# Multi-Objective Smart Charging



- Critical to ensure that *each* of  $J_1, \dots, J_N$  is a *convex function* of  $P^V[t], P^B[t]$ 
  - Some design is needed. Not all desires are naturally represented by a convex function
- **Example:** Our EV-owner-centric smart charging objective function
  - Weighted sum of four convex functionals,  $J_{\{1,2,3,4\}}$ . Weights are user-selectable
  - **minimize**  $w_1 \bar{J}_1 + w_2 \bar{J}_2 + w_3 \bar{J}_3 + w_4 \bar{J}_4$ 
    - Decision variables  $\rightarrow P^V[t], P^B[t]$
    - Min. \$ paid to utility
    - Max. renewable energy consumption
    - Max. EV charging urgency
    - Min. battery degradation
  - **Constraints:** Power balance; EV/storage (dis)charging power limits; Max. power draw from grid; EV/storage battery energy limits, battery dynamics, energy boundary conditions
- **Virtues**
  - Formulation is comprehensive, flexible, allows for human input
  - Problem is *convex by design*: solvers are mature and efficient, revealing tradeoffs is easy
    - Our problem can be expressed as a quadratic program: **minimize**  $\mathbf{x}^T \mathbf{H} \mathbf{x} + \mathbf{f}^T \mathbf{x}$  subject to  $\mathbf{A} \mathbf{x} \leq \mathbf{b}$
    - Checking problem feasibility = solving a linear program: **minimize**  $\mathbf{0}^T \mathbf{x}$  subject to  $\mathbf{A} \mathbf{x} \leq \mathbf{b}$
    - Can choose to solve problem as a *series* of optimization problems (exploiting optimal substructure). This may help overcome uncertainty / unexpected variations in input data, **see our paper!**

Charging urgency and battery degradation can be traded off by varying  $w_3$  and  $w_4$



# Summary, Conclusions



**IECON 2021**  
47<sup>th</sup> Annual Conference of the  
IEEE Industrial Electronics Society  
OCTOBER 13 - 16, 2021 | VIRTUAL CONFERENCE

- Interests of EV owners may not be represented well by a single smart charging objective. EV owner-centric smart charging must therefore be viewed as a multi-objective optimization problem
- We introduced renewable energy consumption as a smart charging objective
  - And borrowed others from the literature to develop a comprehensive and flexible objective function
- We developed a *framework* for treating multi-objective smart charging problems in a single residence
  - We treated the EV owner-centric case, but the ideas apply also to the utility-centric case (see table on Slide 3)
  - We insisted on formulating the smart charging problem as a convex optimization problem
  - Our insistence on a convex problem formulation allowed us to *efficiently* reveal tradeoffs between multiple objectives
  - We also developed a post-processing method to easily present tradeoffs to a human – **see our paper!**
  - Convex problem formulation also has other benefits:
    - Checking problem feasibility is easy
    - May help overcome uncertainty / unexpected variations in input data, **see our paper!**



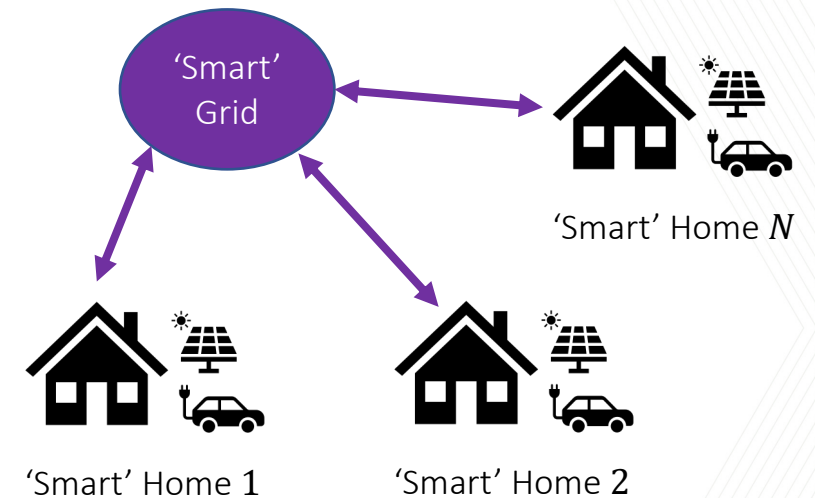
# Next Steps

- We plan to:

- Demonstrate that the power utility can obtain benefits by influencing selection of weights in homes operating independently using the proposed smart charging strategy
- Assess the grid impact of multiple homes operating independently using the proposed smart charging strategy
- Develop a hardware demonstration of smart charging featuring embedded optimization solvers
- Study how to coordinate the charging of multiple EVs without a centralized decision maker
- Study how EV owners and the utility (where both parties self-interested) can interact to address utility-side needs



**IECON 2021**  
47<sup>th</sup> Annual Conference of the  
IEEE Industrial Electronics Society  
OCTOBER 13 - 16, 2021 | VIRTUAL CONFERENCE

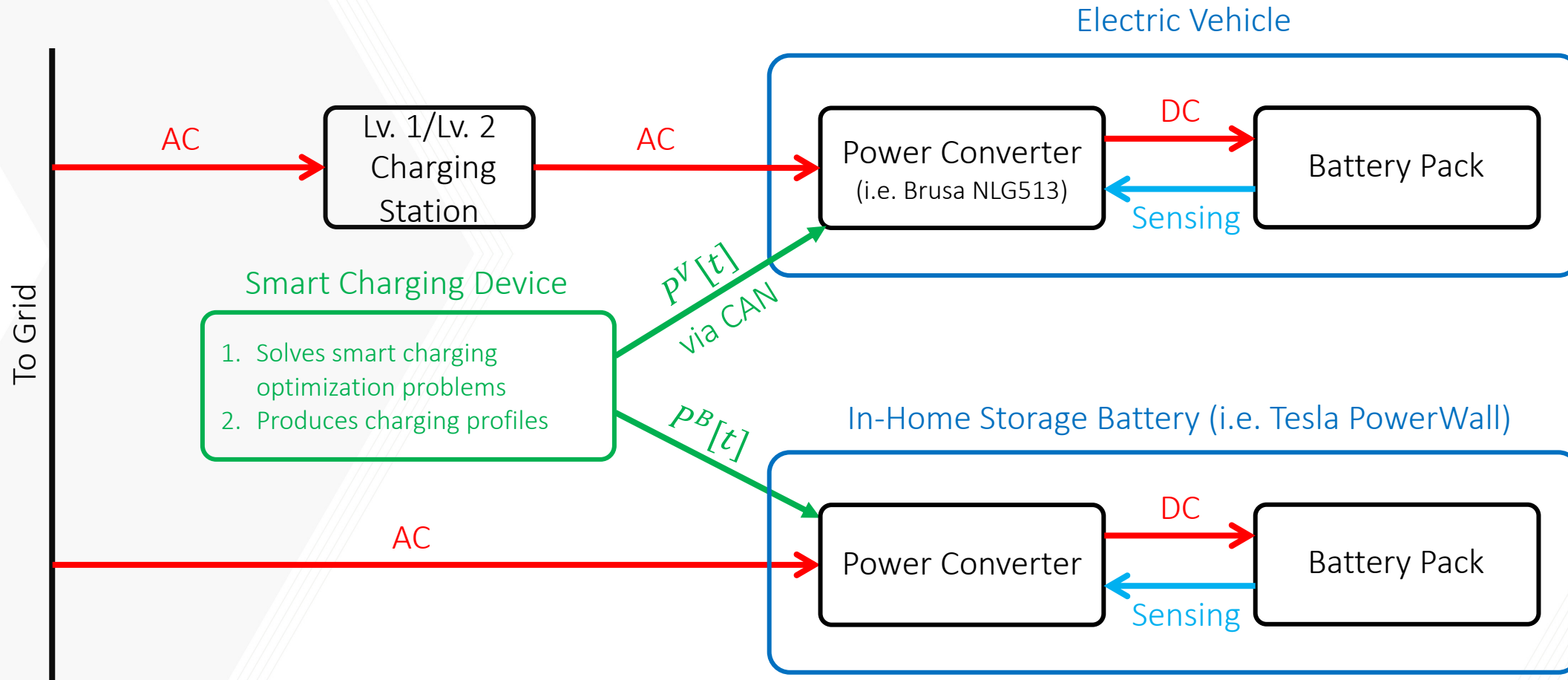


## Thank you for this opportunity!

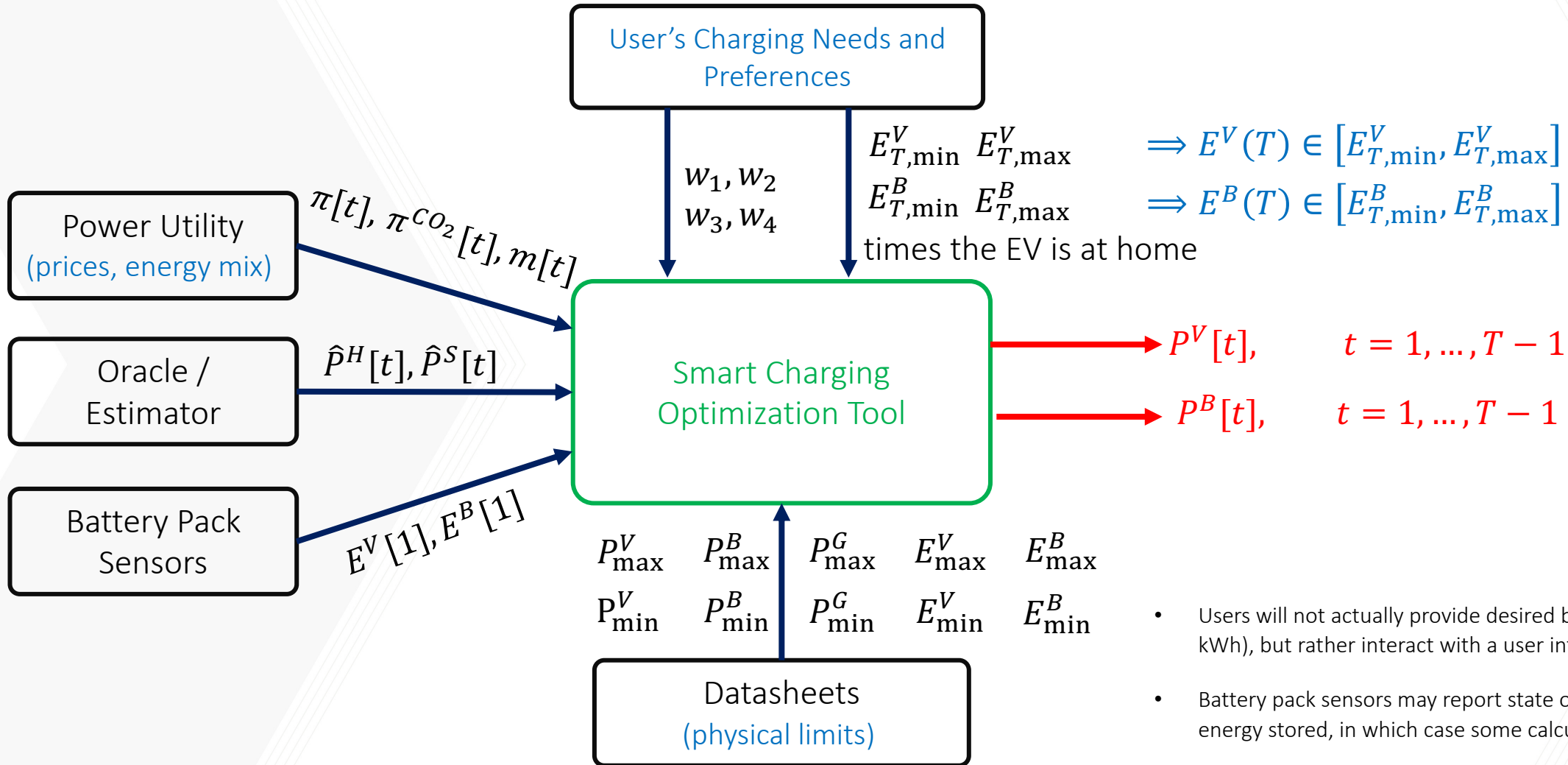
# Details: Smart Charger Integration



- We assume that battery power converters will relinquish authority over (dis)charging to us:



# Details: Data Requirements



- Users will not actually provide desired battery energy levels (in kWh), but rather interact with a user interface
- Battery pack sensors may report state of charge instead of energy stored, in which case some calculations will be needed

# Details: Objective Function



- Four terms:  $J_1, J_2, J_3$ , and  $J_4$ ; User-selectable weights for each term:  $w_1, w_2, w_3$ , and  $w_4$
- All four terms are either linear or quadratic in the optimization variables

- Blue: Decision variable
- Orange: Input data

$$\text{minimize } w_1 J_1 + w_2 J_2 + w_3 J_3 + w_4 J_4$$

$$J_1 = \sum_{t=1}^{T-1} (\pi[t] + \pi^{CO_2}[t]) P^G[t]$$

Min. payments to the utility

$$J_2 = \sum_{t=1}^{T-1} \underbrace{[m[t] P^G[t] + \hat{P}^S[t]]}_{\text{renewable supply}} - \underbrace{[\hat{P}^H[t] + P^V[t] + P^B[t]]}_{\text{total demand}}^2$$

Use up renewable energy

$$J_3 = \sum_{t=1}^{T-1} t P^V[t]$$

Charge EV aggressively

$$J_4 = \sum_{t=1}^{T-1} (P^V[t])^2 + (P^B[t])^2$$

Min. battery degradation



# Details: Constraints



- Blue: Decision variable
- Orange: Input data

- All constraints are linear in the optimization variables.

Can be < 0 if  
bidirectional  
power flow  
allowed

For  $t = 1, \dots, T$ :

$$P^G[t] + \hat{P}^S[t] = P^V[t] + P^B[t] + \hat{P}^H[t]$$

$$P_{\min}^G \leq P^G[t] \leq P_{\max}^G$$

$$P_{\min}^V \leq P^V[t] \leq P_{\max}^{EV}$$

$$P_{\max}^B \leq P^B[t] \leq P_{\max}^B$$

$$E_{\min}^V \leq E^V[t] \leq E_{\max}^V$$

$$E_{\min}^B \leq E^B[t] \leq E_{\max}^B$$

For  $t = 1, \dots, T - 1$ :

$$E^V[t + 1] = E^V[t] + \Delta P^V[t]$$

$$E^B[t + 1] = E^B[t] + \Delta P^B[t]$$

For  $t = 1, T$ :

$$E^V[1] \text{ specified, } E^V[T] \in [E_{T,\min}^V, E_{T,\max}^V]$$

$$E^B[1] \text{ specified, } E^B[T] \in [E_{T,\min}^B, E_{T,\max}^B]$$

Power balance

Limits on power flow to/from grid

Limits on power flow to/from batteries

Limits on energy stored in batteries

Battery dynamics

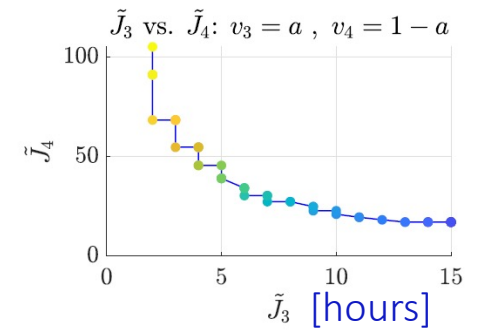
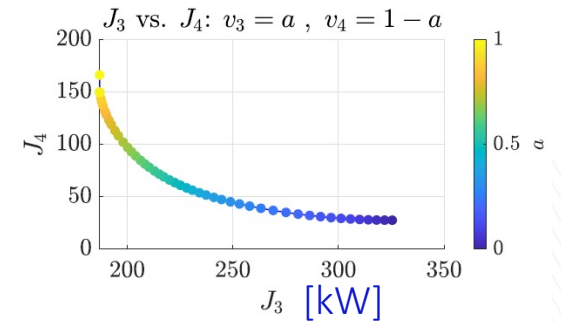
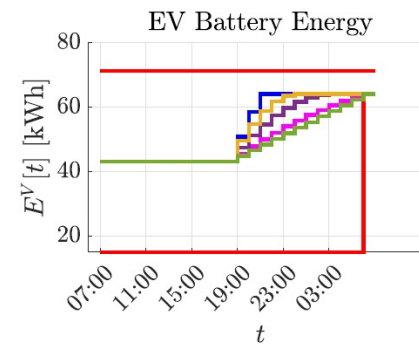
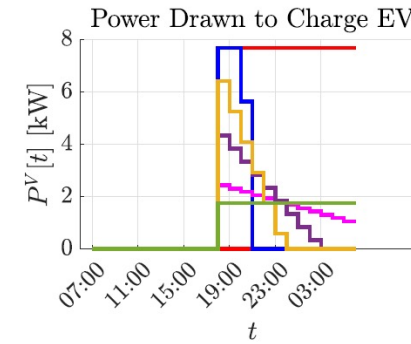
Boundary conditions

(either auto-specified, or obtained from user)

# Details: Revealing Tradeoffs



- Objective function terms designed to be convex, not necessarily to be easily-interpretable
  - E.g. minimizing  $J_3(P^V) = \sum_{t=1}^{T-1} t P^V[t]$  will charge the EV as fast as possible, but  $J_3$  does not have units of time
- Change how we present the tradeoffs to a human by post-processing Pareto-optimal solutions
  - Each Pareto optimal solution corresponds to a charging schedule
  - Charging schedule can be used to evaluate more easily interpretable performance functionals (proxy functionals)
  - Create *up to two* functionals to represent a particular smart charging objective/desire



Convex Functional	Interpretable Functional
Not necessarily most interpretable	Not necessarily a convex function of decision variables
Used for solving smart charging optimization problems and revealing tradeoffs	Used to post-process solutions and reveal tradeoff curves with interpretable units

Example from paper in which charging urgency ( $J_3, \tilde{J}_3$ ) and battery degradation ( $J_4, \tilde{J}_4$ ) are traded off

Aside:  $v_3$  and  $v_4$  are related to  $w_3$  and  $w_4$ . Some details are omitted in this presentation